## Date:

Objective: I will graph data to determine proportional relationships.

## Vocabulary

Proportional Relationship: a relationship between two equal ratios

| Apples | Cost (\$) |
| :---: | :---: |
| 5 | 2 |
| 20 | 8 |


*The graph of a proportional relationship is a line that passes through the origin $(0,0)$.

Ordered Pair: a pair of numbers used to locate a point on a coordinate plane; also, called the coordinates

$$
\begin{gathered}
(4,3) \\
(x, y) \\
\text { (horizontal, vertical) }
\end{gathered}
$$

## Steps:

1. Convert data to ordered pairs.
2. Draw a coordinate plane.
3. Plot ordered pairs on the coordinate plane.
4. Draw a line connecting the points.
5. If the line goes through the origin $(0,0)$, the relationship is proportional.

## Example \# 1

Directions: Use a graph to answer the following.
Convert the entries in the table to ordered pairs, plot the coordinates on the coordinate plane, and determine which points lie on a straight line with the origin.

| $x$ | $y$ |
| :---: | :---: |
| 1 | 1 |
| 2 | 3 |
| 3 | 3 |

## Solution:

- Add a third column to the table to identify the given coordinate points.

| $\boldsymbol{x}$ | $\boldsymbol{y}$ | $(x, y)$ |
| :---: | :---: | :---: |
| 1 | 1 | $(1,1)$ |
| 2 | 3 | $(2,3)$ |
| 3 | 3 | $(3,3)$ |

- Plot the given coordinates. Using a straight line to connect the points that have a proportional relationship.

- The points $(1,1)$ and $(3,3)$ lie on the straight line with the origin.


## Example \# 2

The table below gives the dimensions of two rectangular prisms. Are the prisms in proportion? How does it help to create a graph?

|  | Prism 1 | Prism 2 |
| :--- | :---: | :---: |
| Length | 20 cm | 24 cm |
| Width | 15 cm | 18 cm |
| Height | 17.5 cm | 21 cm |

## Solution:

- Add a third column to the table to identify the given coordinate points.

|  | Prism 1 <br> $\boldsymbol{x}$ | Prism 2 <br> $\boldsymbol{y}$ | $(\boldsymbol{x}, \boldsymbol{y})$ |
| :--- | :---: | :---: | :---: |
| Length | 20 cm | 24 cm | $(20,24)$ |
| Width | 15 cm | 18 cm | $(15,18)$ |
| Height | 17.5 cm | 21 cm | $(17.5,21)$ |

- Plot the given coordinates. Using a straight line connect the points that have a proportional relationship.

- Yes, the prisms are in proportion.
- A graph helps you see that a straight line can be drawn through all three points and the origin.
$\qquad$

Directions: Graph to answer the following.

1. Is the number of math problems Jon can complete in proportion to the amount of time he works?

| Time | \# of Problems | $(x, y)$ |
| :---: | :---: | :---: |
| 30 min | 10 |  |
| 20 min | 15 |  |
| 15 min | 7 |  |


3. Which triangles, if any, are in proportion to each other?

|  | Height | Base | $(\boldsymbol{x}, \boldsymbol{y})$ |
| :--- | :---: | :---: | :---: |
| Triangle A | 6 | 3 |  |
| Triangle B | 10 | 4 |  |
| Triangle C | 2.5 | 1 |  |


2. Is the number of math problems Ron can complete in proportion to the amount of time he works?

| Time | \#of Problems | $(\boldsymbol{x}, \boldsymbol{y})$ |
| :---: | :---: | :---: |
| 20 min | 10 |  |
| 30 min | 15 |  |
| 14 min | 7 |  |

4. Which rectangles, if any, are in proportion to each other?

|  | Length | Width | $(\boldsymbol{x}, \boldsymbol{y})$ |
| :--- | :---: | :---: | :---: |
| Rectangle A | 20 | 15 |  |
| Rectangle B | 48 | 36 |  |
| Rectangle C | 21 | 18 |  |


5. Is the amount of money earned proportional to the number of hours worked?

|  | Hours | Earnings | $(x, y)$ |
| :--- | :---: | :---: | :---: |
| Fred | 10 | $\$ 150$ |  |
| Ted | 12 | $\$ 252$ |  |
| Ned | 15 | $\$ 150$ |  |

6. Is the amount of money earned proportional to the number of hours worked?

|  | Hours | Earnings | $(\boldsymbol{x}, \boldsymbol{y})$ |
| :--- | :---: | :---: | :---: |
| Lillie | 10 | $\$ 120$ |  |
| Millie | 7 | $\$ 84$ |  |
| Tillie | 14 | $\$ 168$ |  |

Explain the steps you used to solve problem number $\qquad$ .
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

